



DYNAMIC FINITE ELEMENT AND DYNAMIC PHOTOELASTIC ANALYSES

OF AN IMPACTED PRETENSIONED PLATE

by

A.S. Kobayashi, S. Mall and A.F. Emery

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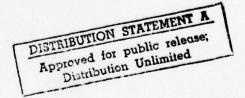


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# DYNAMIC FINITE ELEMENT AND DYNAMIC PHOTOELASTIC ANALYSES OF AN IMPACTED PRETENSIONED PLATE

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# ABSTRACT

ESSO type fracture toughness specimen machined from Homalite-100 sheets of 9.5mm thickness. Crack velocities determined from photoelasticity experiments were prescribed in the dynamic finite element analysis for the purpose of establishing numerically a dynamic fracture toughness which varies with the crack velocity. Qualitative agreement between dynamic energy release rates determined by the two procedures were found, provided an appropriate impulse was prescribed in the dynamic finite element analysis. The dynamic finite element analysis also provided results with sufficient time resolution to confirm our postulate that  $K_d = K_c$  at the onset of crack propagation in Homalite-100 plates and that  $K_a$  varies in these test specimens.

# INTRODUCTION

Two popular test specimens used in studying crack arrest potential of structure steel are the ESSO and Robertson specimens [1,2]\* in which dynamic crack propagation is initiated through impacting a wedge in the crack of a subcritically loaded single-edged notch tension plate. Crack arrest in these experiments is attained at regions of either higher fracture toughness generated by higher local temperature in low carbon steel specimen and/or lower stress intensity factors generated by lower local stress field.

<sup>\*</sup> Denotes references at the end of this paper.

Previous dynamic photoelastic analysis of ESSO type test specimens modeled by Homalite-100 plates [3] showed that the dynamic effects of the propagating crack combined with that of the impacting projectile have considerable effect on the dynamic stress intensity factor and hence on crack propagation. Unfortunately, these results neither provided a unique relation between the crack velocity and dynamic fracture toughness nor an insight into the basic mechanism of crack arrest. In addition, the results are not in complete agreement with the more recent experimental results obtained on thicker Homalite-100 plates [4,5].

In order to verify, by an independent procedure, some of the controversial results obtained during our past seven-year efforts in fracture dynamics, the authors have used a relatively simple dynamic finite element code to duplicate some of their past work in dynamic photoelasticity [6,7,8]. Encouraged by the reasonable agreements between the numerical and experimental results obtained through this series of studies involving single-edged notch specimens loaded to criticality, the same dynamic finite element code was used to analyze the previous dynamic photoelastic results on the ESSO type test specimens [3].

# DYNAMIC PHOTOELASTIC ANALYSIS

The dynamic photoelastic experiments in this paper involve subcritically loaded single-edged notch tension specimens where crack propagation was initiated by an impacted flat-nosed projectile or a 65° wedge. The test specimens consisted of a 9.53mm (3/8 in.) thick Homalite-100 plate with a 0.254 x 0.254m (10 in. x 10 in.) test section loaded in a fixed gripped condition with uniform grip displacement, and with a single-edged starter crack approximately 9.53mm (3/8 in.) in length. The dynamic properties of Homalite-100 were obtained following the procedure of Clark and Sanford [9], which yielded an average dynamic modulus of

of elasticity, Poisson's ratio and stress optic coefficient of 4650 N/mm<sup>2</sup> (675 ksi), 0.345 and 27.2 N/mm<sup>2</sup> fringe (155 psi-in/fringe), respectively.

The averaged static fracture toughness, which was obtained through separate tests using SEN specimens, was 20.1 N/mm<sup>3/2</sup> (579 psi√in).

Figure 1 shows 15 frames (1 frame misfired) of dynamic photoelastic patterns obtained by impacting a subcritically loaded single-edged crack plate with a flat nose projectile from the bottom. Note that the crack propagated along a curved path indicating that the crack was driven by the stress waves generated by the impact on this subcritically loaded plate.

Dynamic stress intensity factors,  $K_D$ , were determined by Bradley's two parameter procedure [10] and the dynamic energy release rate,  $\mathcal{L}_D$ , was computed using Freund's equation [11] from the dynamic stress intensity factors. Further details of these data reduction schemes can be found in References 6 and 8.

# DYNAMIC FINITE ELEMENT ANALYSIS

The dynamic finite element code, HONDO [12], used in this investigation is based on on explicit time integration scheme and constant strain quadrilateral elements. The crack tip motion was modeled by discontinuous jumps where the crack tip moved from one finite element node to another at discrete time intervals. This discrete propagation of the crack tip generated significant oscillations in the states of stress and displacement surrounding the crack tip. The numerical noise was filtered by computing directly the dynamic energy released by the discrete crack tip advancement from the time-averaged normal stress ahead of the advancing crack tip and the corresponding time-averaged crack opening displacement after crack advance. Details of this numerical procedure as well as an accuracy check of the procedure are described in Reference 6.

Figure 2 shows the finite element breakdown involving a total of 532 elements

and 585 nodes used in this analysis. Impacted wedge-loading was simulated by two simultaneously applied vertical and horizontal forces at the crack mouth without the wedge-shape and the impact forces for the flat nose projectile and 65° wedge were assumed to vary with impact duration. Large plastic deformations at the impact sites were assumed to dissipate about 66 percent and 43 percent of the impact energies for the flat nose and 65° wedge impacts, respectively. Estimates of these energy losses as well as impact durations were made by comparing the calculated dynamic maximum shear stress patterns of a given impulse with the associated dynamic isochromatic patterns along the plate axis of symmetry as shown in Figure 3 and the calculated and measured maximum stresses along the free edge of the specimen as shown in Figure 4. Note that Figures 3 and 4 compare the calculated and measured results in the vicinity of the impact point only and thus one could conclude that the agreements are fair in view of the rapid variations in stresses in this region. As shown in Figure 3, the differences between the calculated and measured stresses decrease rapidly away from the impact point and thus better agreement between the two is to be expected in the region removed from the impact point.

# PRETENSIONED SINGLE-EDGED NOTCH PLATE IMPACTED BY FLAT NOSE PROJECTILE

In the series of dynamic photoelastic experiments reported in Reference 3, the crack propagated in some pretensioned single-edged notch plates while it did not run in others. These stop-or-go results potentially provided information for estimating the static fracture toughness under stress-wave loadings but unfortunately the dynamic photoelastic patterns prior to crack propagation were not recorded in these experiments. A combination of dynamic finite element analysis and dynamic photoelasticity results, however, provided a procedure in which the dynamic state prior to the triggering of the dynamic photoelasticity

system could be estimated by some trial and error. Figure 5 shows such variations in dynamic stress intensity factors due to impact for a stationary crack in Test No. W012172 and prior to crack propagation in Test Nos. W020672 and W090771.

It is interesting to note that in Test No. W012172 in which the crack remained stationary the calculated dynamic energy release rate,  $I_D$ , is barely equal to or lower than the critical strain energy release rate,  $I_C$ .  $I_D$  exceeds  $I_C$  within 20 microseconds after impact and is in agreement with the estimated time at which the crack started to propagate in the dynamic photoelasticity experiments. This combined dynamic photoelasticity-dynamic finite element analysis indicates that the crack initiation dynamic fracture toughness,  $I_C$  under this combined static and stress wave loading is close to, within experimental scatters, the static fracture toughness of  $I_C$  = 20.1 N/mm $I_C$  (579 psi $I_C$ in). Perhaps such coincidence may be expected in view of the recent work by G.C. Smith [13] who found that the variations in fracture toughness of 4.76mm (3/16 in.) thick Homalite-100 plates is approximately equal to the static fracture toughness for the time interval to failure of 20 microseconds. The 30-50 percent increase in stress intensity factor due to impulse loading falls within the rapidly changing dynamic fracture toughness at this time interval to failure.

# PRETENSIONED SINGLE-EDGED NOTCH PLATE IMPACTED BY A 65° WEDGE

The dynamic photoelasticity record of Test No. W012472 was analyzed then by the dynamic finite element method using the idealized crack velocity shown in Figure 6. Figure 7 shows the variations in computed dynamic energy release rates due to various impulses used. Figure 8 shows the final impulse used in analyzing this experiment as well as the computed and measured dynamic energy release rates and the computed static strain energy release rate without the

DISCUSSIONS

impulse. Momentary crack arrest at a/b  $\stackrel{.}{=}$  0.39 in the presence of a static strain energy release rate which exceeds  $\frac{\textbf{y}}{c}$  underscores the importance of dynamic analysis in studying the crack arrest phenomenon under such dynamic loading conditions.

In this study the importance of a correct impulse shape for computing the dynamic energy release rate has been underscored by the sensitivity of dynamic stress intensity factor, K<sub>D</sub>, to the varying state of stress which was governed by the applied impulse. Unfortunately, the muzzle velocity measurements of the projectile were unreliable and the subtle variabilities in contact conditions between the projectile and plate appeared to have significant influence on the impulse shape. As a result, considerable amount of trial and error was necessary to arrive at a suitable impulse to match the computed and measured dynamic energy release rates. Such trial and error defeats the original intent of using dynamic finite element method as an independent check of our past dynamic photoelasticity results. Nevertheless, the dynamic finite element analysis served to verify the following.

Our previous conclusion, which was discussed in Reference 7 involving simulated dynamic tear tests, that the fracture toughness at crack initiation did not differ with its static counterpart, appears to be also valid under combined static and impulse loadings. As mentioned previously, these findings are in agreement with those in Reference 13 because of the relatively low strain rate effects involved in these tests.

The dynamic energy release rate at crack arrest was much lower than those measured in non-impact experiments [7] which again reinforces our postulate that  $\mathcal{A}_D$  at crack arrest is not a material property. The average dynamic energy release rate, which is obtained by dividing the sum of the total dynamic energy release rates by the newly created crack surface by crack propagation, for Test W012472,

yielded 2 = 2.33 and 2.28 from the dynamic photoelasticity and dynamic The large Dlave generated by elastic analysis FEM analysis, respectively. for a prescribed crack propagation history probably indicates the larger dissipation in dynamic energy due to viscous damping and at the flexible edge grips under high impact loading.

# ACKNOWLEDGEMENT

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Figure 1. Dynamic Photoelastic Patterns of a Propagating Crack in a Single-Edged Crack Pretensioned Plate Impacted by a Flat Nose Projectile. Test No. W090771 Crack missed the 3.8 mm dia. hole located at the center of the plate.

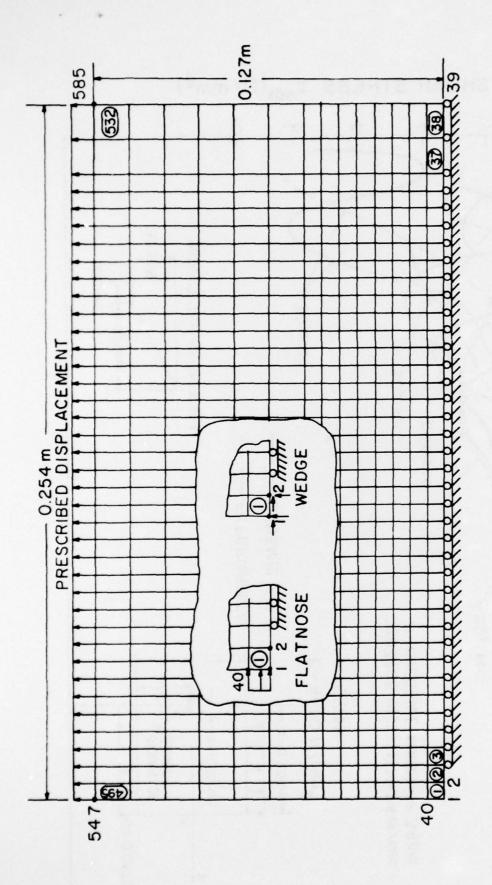
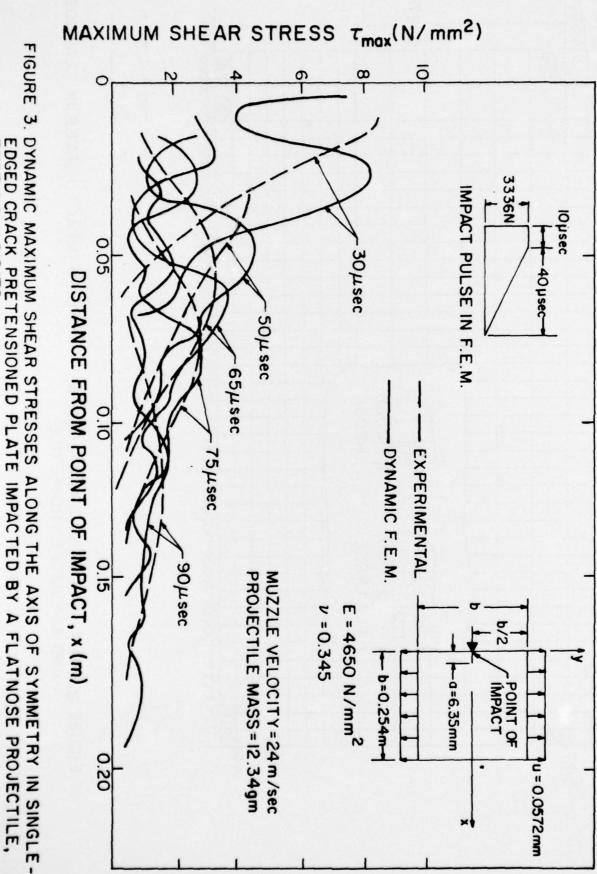


FIGURE 2. FINITE ELEMENT BREAKDOWN WITH APPLIED IMPACT FORCES IN FLATNOSE AND 65° WEDGE PROJECTILE.



EDGED CRACK PRETENSIONED PLATE IMPACTED BY A FLATNOSE PROJECTILE, TEST NO. WOI2172

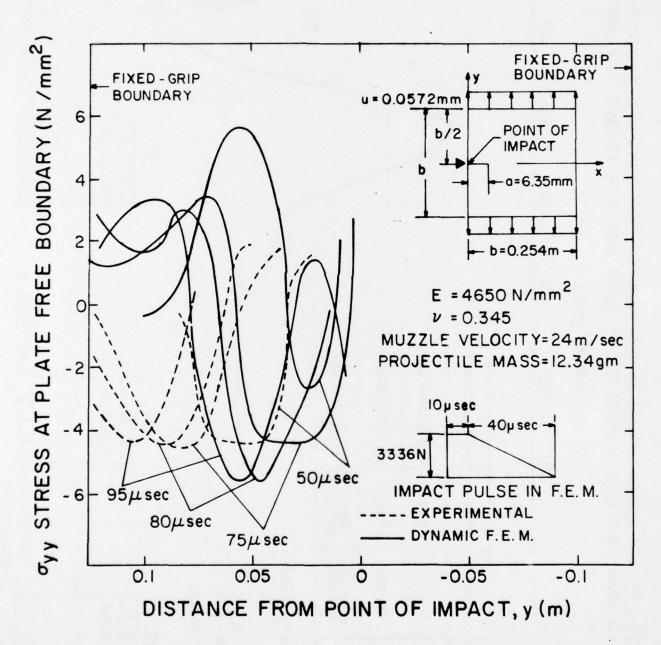


FIGURE 4. DYNAMIC MAXIMUM STRESS, σyy, ALONG A FREE BOUNDARY IN SINGLE - EDGED CRACK PRETENSIONED PLATE IMPACTED BY A FLATNOSE PROJECTILE, TEST NO. WOI2172.

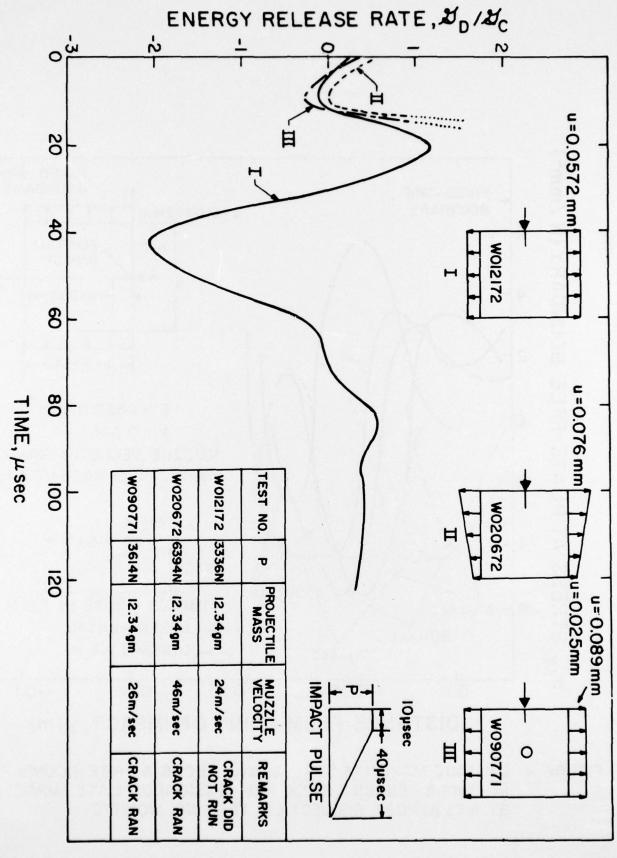


FIGURE 5. NUMERICAL ENERGY RELEASE RATE AFTER IMPACT IN THREE SINGLE - EDGED CRACK PRETENSIONED PLATES IMPACTED BY A FLATNOSED PROJECTILE.

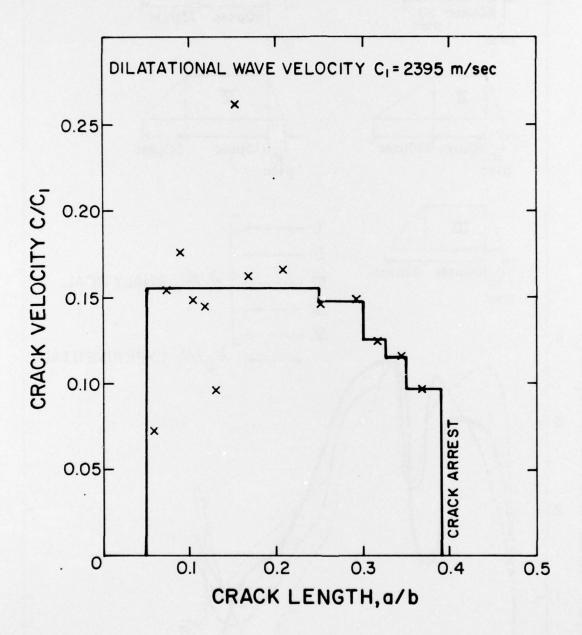


FIGURE 6. CRACK VELOCITIES USED FOR NUMERICAL ANALYSIS ALONG WITH EXPERIMENTAL DATA, TEST NO. WOI2472

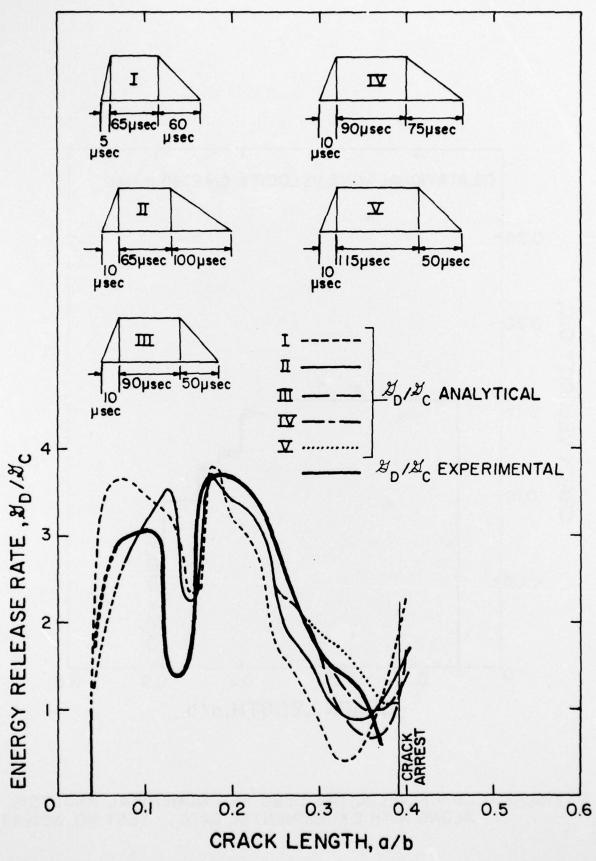


FIGURE 7. ENERGY RELEASE RATES FOR VARIOUS IMPACT PULSES, TEST NO. WO12472

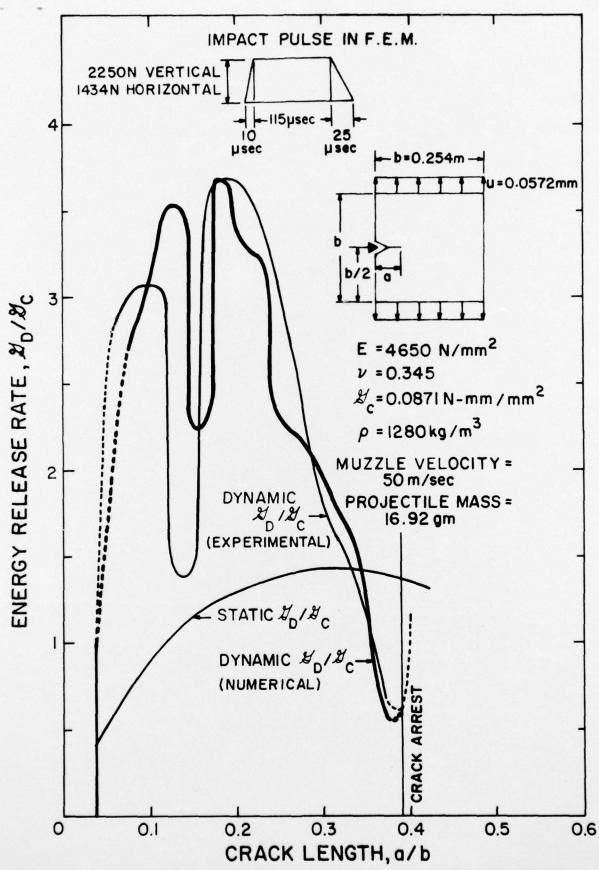


FIGURE 8. ENERGY RELEASE RATES IN A SINGLE - EDGED CRACK PRETENSIONED PLATE IMPACTED BY A 65° WEDGE, TEST NO. WO12472

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NABSTRACT (Continue on reverse side if necessary and identify by block number)	
Dynamic finite element and dynamic photoelasticit	
type fracture toughness specimer machined from Ho	malite-100 sheets of 9 5mm
thickness. Crack velocities determined from phot	oelasticity experiments were
prescribed in the dynamic finite element analysis	for the purpose of establish-
ing numerically a dynamic fracture toughness whic	h varies with the crack velo-
city. Qualitative agreement between dynamic ener	gy release rates determined
by the two procedures were found, provided an app	ropriate impulse was prescribed
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in the dynamic finite element analysis. The dynamic finite element analysis also provided results with sufficient time resolution to confirm our postulage that Ka = K at the onset of crack propagation in Homalite-100 plates and that Ka varies in these test specimens.

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